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program test
use fmzm

! fm_find_min is a multiple precision function minimization routine that uses Brent's method.

! The function to be minimized or maximized is f(x, nf).
! x is the argument to the function.
! nf is the function number in case extrema to several functions are needed.

implicit none
character(80) :: st1, st2

! Declare the multiple precision variables.

type (fm), save :: a, b, tol, xval, fval
type (fm), external :: f

! Set the FM precision to 50 significant digits (plus a few more "guard digits")

call fm_set(50)

! Find a minimum of the first function, x**3 - 9*x + 17.
! a, b are two endpoints of an interval in which the search takes place.

a = 1
b = 2

! tol is the error tolerance.

tol = epsilon(a)

write (*,*) ' '
write (*,*) ' '
write (*,*) ' Case 1. Call fm_find_min to find a relative minimum between 1 and 2'
write (*,*) ' for f(x) = x**3 - 9*x + 17.'
write (*,*) ' Use kprt = 0, so no output will be done in the routine, then'
write (*,*) ' write the results from the main program.'

! For this call no trace output will be done (kprt = 0).

call fm_find_min(1, a, b, tol, xval, fval, f, 1, 0, 6)

! Write the result, using f52.50 format, and compare xval to the true minimum, sqrt(3).

call fm_form('f52.50', xval, st1)
call fm_form('f52.50', fval, st2)
write (*, "(/' A minimum for function 1 is/' x = ', a/' f(x) = ', a)") &
trim(st1), trim(st2)
call fm_form('es17.10', abs(xval-sqrt(to_fm(3))), st2)
write (*, "(/' Error for x = ',a)") trim(st2)

! Find a maximum of the first function, x**3 - 9*x + 17.

! This time we use fm_find_min's built-in trace (kprt = 1) to print the final
! approximation to the root. The output will appear on more than one line, to
! allow for the possibility that precision could be hundreds or thousands of digits,
! so the number might not fit on one line.

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write (*,*) ' '
write (*,*) ' '
write (*,*) ' Case 2. Find a relative maximum between -5 and 1.'
write (*,*) ' Use kprt = 1, so fm_find_min will print the results.'

call fm_find_min(2, -to_fm('5.0d0'), to_fm('1.0d0'), tol, xval, fval, f, 1, 1, 6)

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! Find a maximum of the first function,  $x^3 - 9x + 17$ .

! See what happens when the maximum value is at an endpoint of the search interval.
! The algorithm still finds a relative maximum in the interior of the interval,
! not the absolute maximum at  $x=5$ .

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write (*,*) ' '
write (*,*) ' '
write (*,*) ' Case 3. Find a relative maximum between -5 and 5.'
write (*,*) ' Use kprt = 2, so fm_find_min will print all iterations,'
write (*,*) ' as well as the final results.'

call fm_find_min(2, -to_fm('5.0d0'), to_fm('5.0d0'), tol, xval, fval, f, 1, 2, 6)

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! Find a minimum of the second function,  $\gamma(x)$ .

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write (*,*) ' '
write (*,*) ' '
write (*,*) ' Case 4. The gamma function has one minimum for positive x.'
write (*,*) ' Find it, printing all iterations.'

call fm_find_min(1, to_fm('0.1d0'), to_fm('3.0d0'), tol, xval, fval, f, 2, 2, 6)

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write (*,*) ' '

end program test

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function f(x, nf) result (return_value)
use fmzm

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! x is the argument to the function.
! nf is the function number.

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implicit none
integer :: nf
type (fm) :: return_value, x
intent (in) :: x, nf

if (nf == 1) then
return_value = x**3 - 9*x + 17
else if (nf == 2) then
return_value = gamma(x)
else
return_value = 3*x**2 + x - 2
endif

end function f

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